

Handout: Limits, Part I

Discussions 201, 203 // 2018-09-07

Problem 1 (Conceptual questions).

- (1) True or false: if the numbers $f(1), f(0.1), f(0.01), f(0.001), \dots$ tend towards 3, then $\lim_{x \rightarrow 0} f(x) = 3$.
- (2) Give an example of a function f and a number a such that the values of $f(a), \lim_{x \rightarrow a^+} f(x)$, and $\lim_{x \rightarrow a^-} f(x)$ are all *different*. (You can just draw the graph of such a function.)
- (3) When $\lim_{x \rightarrow a^+} f(x)$ differs from $\lim_{x \rightarrow a^-} f(x)$, what can we conclude about $\lim_{x \rightarrow a} f(x)$?
- (4) Is it true that $\lim_{x \rightarrow a} f(x) = f(a)$ for any f and any a ?

Problem 2 (Limit evaluation). Determine whether the limit exists, and if it does, evaluate it.

- (1) $\lim_{x \rightarrow 3} (x^3 + 2x - 7)$
- (2) $\lim_{x \rightarrow 0} \frac{x^7 + x^4 + x^2}{5x^4 + x^3 + 5x}$
- (3) $\lim_{x \rightarrow 0} \frac{x^7 + x^4 + x}{5x^4 + x^3 + 5x^2}$
- (4) $\lim_{x \rightarrow 2} \frac{x^2 + x - 6}{x^2 - 4}$
- (5) $\lim_{x \rightarrow \pi/2} ((x - \pi/2) \cos(x))$
- (6) $\lim_{x \rightarrow \pi/2} \left((x - \pi/2) \cos \left(\frac{1}{x - \pi/2} + x^3 - 17 \right) \right)$
- (7) $\lim_{x \rightarrow 0} \left(\frac{\sqrt{2x+1}}{x} - \frac{1}{x} \right)$